

# **Speeding Up Bitcoin**

**David Tse**

**Padovani Lecture**

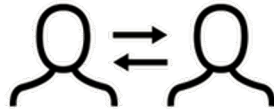
**NASIT 2021**

**June 25, 2021**

# **Part I:**

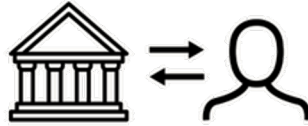
# **Introduction**

# Trust: a basic human need



PHASE 1

TRIBAL TRUST



PHASE 2

INSTITUTIONAL TRUST



PHASE 3

DISTRIBUTED TRUST

- large-scale
- decentralized
- permissionless

# Basis of trust

- An important basis of trust is a common immutable **record of history** that everyone can agree on.
- A challenge of achieving decentralized trust is how to maintain this record of history without a central authority.
- The heart of decentralized trust is a distributed **consensus** problem.

# Decentralizing trust: two breakthroughs

2008

**Bitcoin: A Peer-to-Peer Electronic Cash System**

Satoshi Nakamoto  
satoshin@gmx.com  
www.bitcoin.org

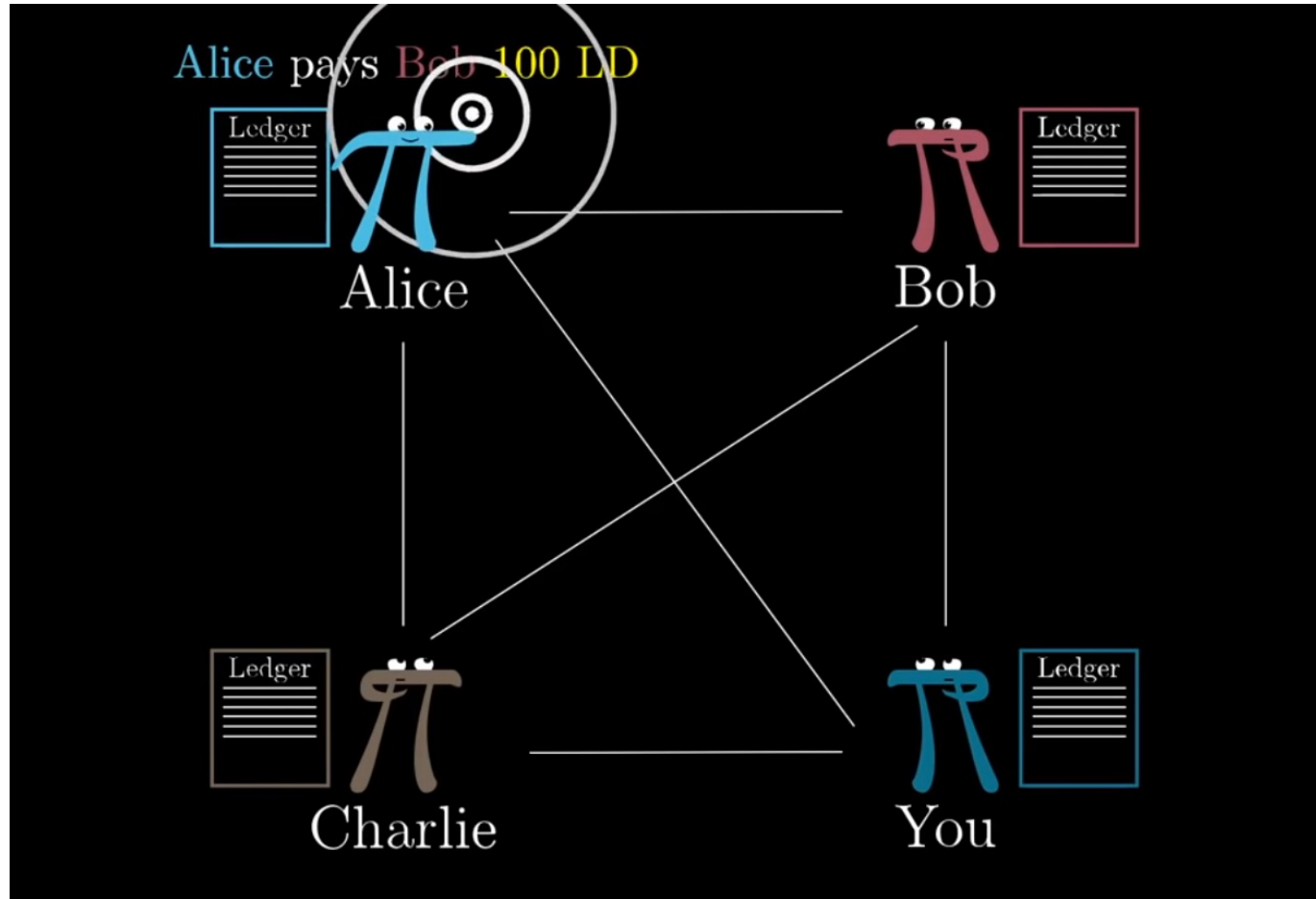
First system to achieve  
large-scale permissionless  
consensus

2013

**Ethereum: The Ultimate Smart Contract and Decentralized Application Platform**

Broaden from payments to other applications

# Bitcoin: a decentralized ledger



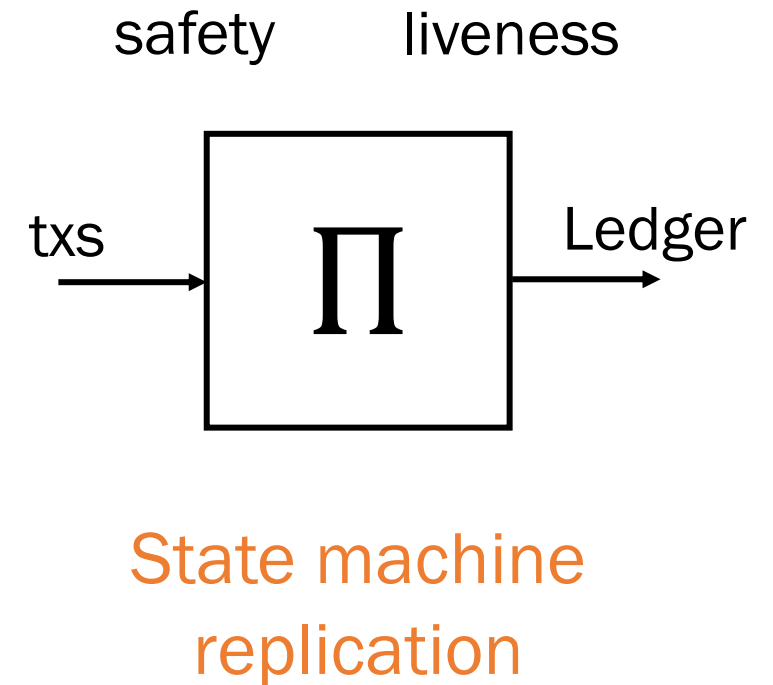
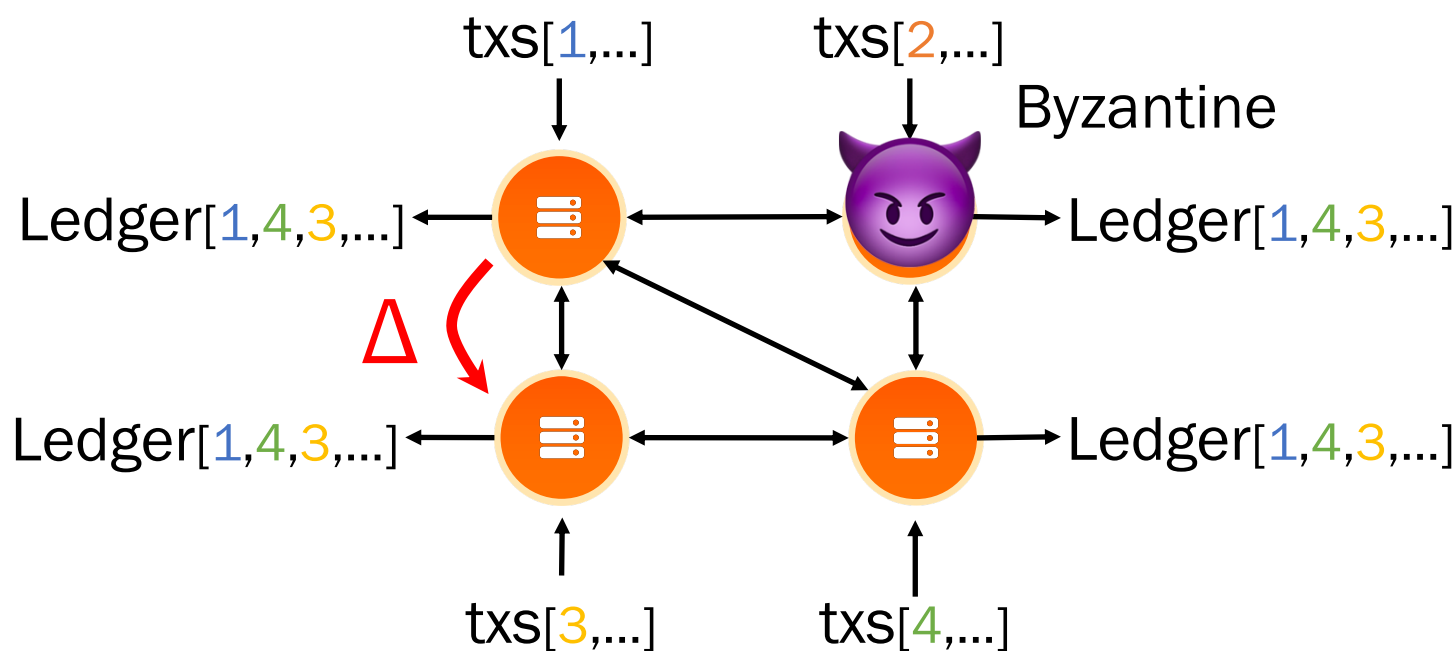
"But how does bitcoin actually work?", Youtube

# **Core problem Bitcoin solved: consensus**

- A new data structure: blockchain
- A new consensus protocol: proof-of-work longest chain protocol

# The Byzantine consensus problem

Lamport, Pease, Shostak 1980, 1982



Typical theorem: a consensus protocol is safe and live when no more than  $f$  out of  $n$  nodes are Byzantine.



# What's new about Bitcoin?

- Traditional consensus protocols are designed for a **closed** environment with a **fixed** set of permissioned nodes.
- Bitcoin is designed for an Internet-scale **open** environment where any node **can join or leave at any time**.

# Permissionless dynamic participation



Theorem: Bitcoin is safe and live when no more than 50% of the online compute power is adversarial.

# Bitcoin: Pros and Cons

## Pros:

- permissionless
- dynamic participation
- Extremely simple protocol

## Cons:

- high consumption of energy (~ Sweden)
- low transaction throughput (7 transactions per second)
- high confirmation latency ( hours)
- No accountability
- Insecure under network partition.

# Questions we will answer

- How does Bitcoin work?
- How do we formalize safety and liveness and how do we prove that Bitcoin is secure?
- Why does Bitcoin have very bad latency?
- How to speed up Bitcoin while keeping its security properties?

# **Part II:**

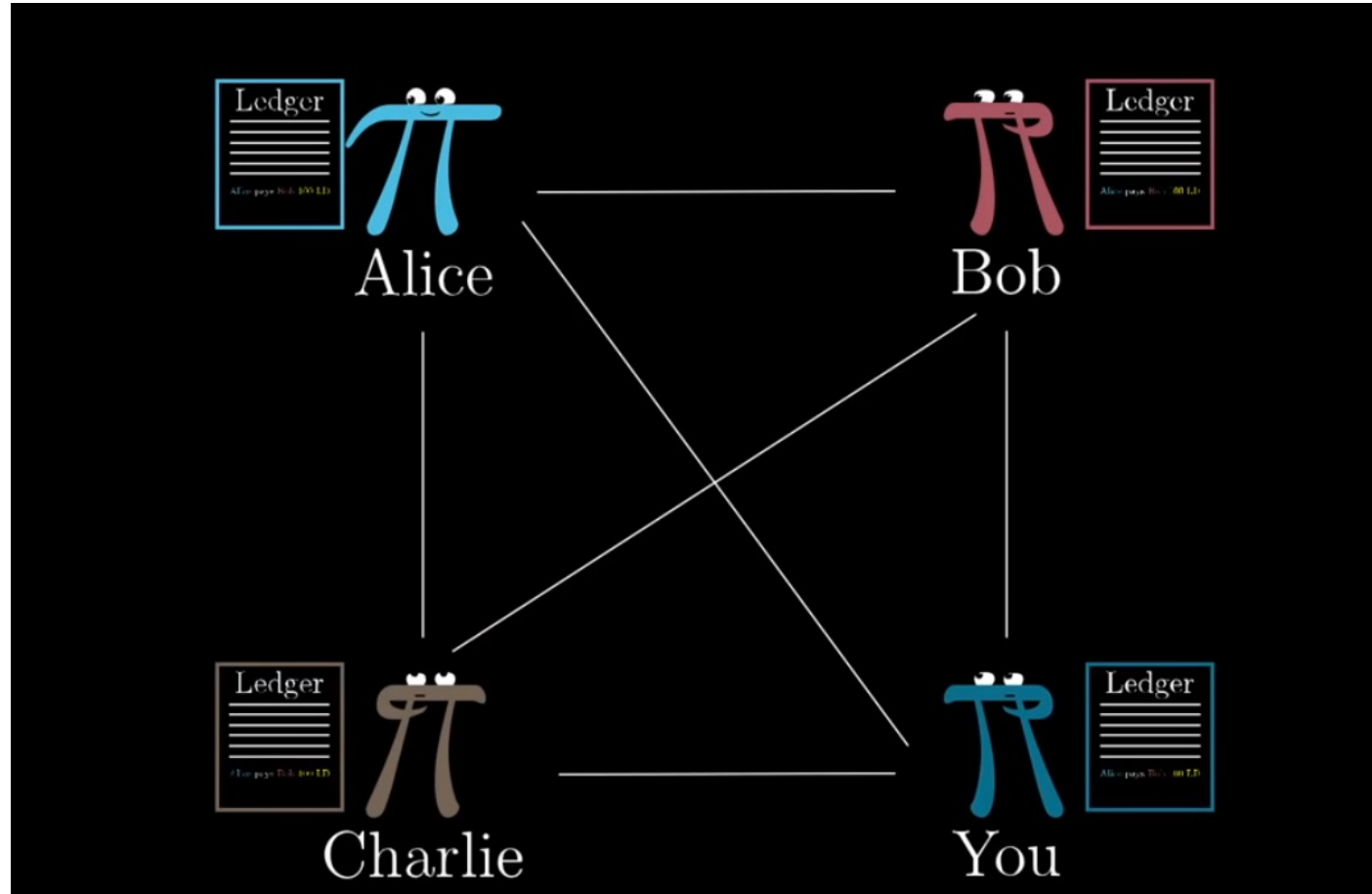
# **Bitcoin and its Security**

# Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto  
satoshin@gmx.com  
www.bitcoin.org

**Abstract.** A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone.

# Ledger



# Data integrity and data agreement

- Data integrity: Data is legit.
  - Solved by digital signatures.
- Data agreement: among all nodes and across time.
  - This is the “double spending” problem and is solved by a consensus protocol.

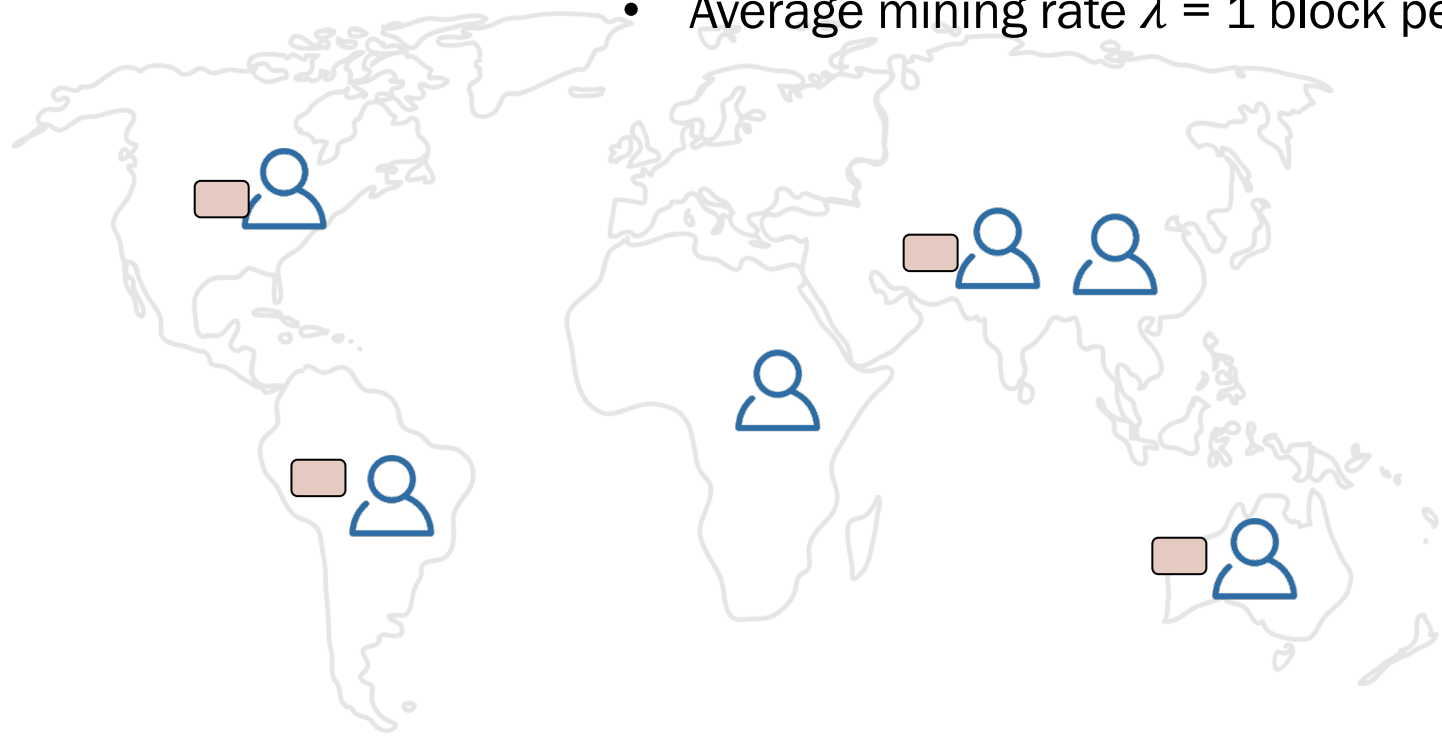
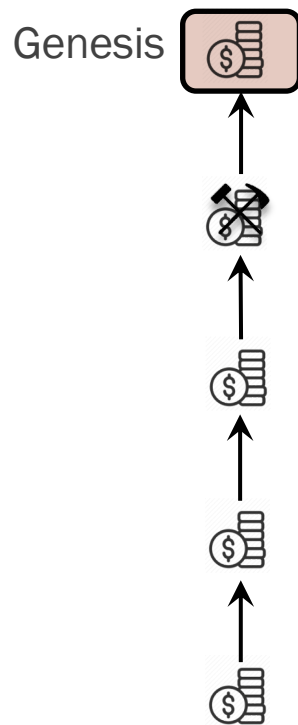


# Protocol

- Mining rule (encoder)
- Confirmation rule (decoder)

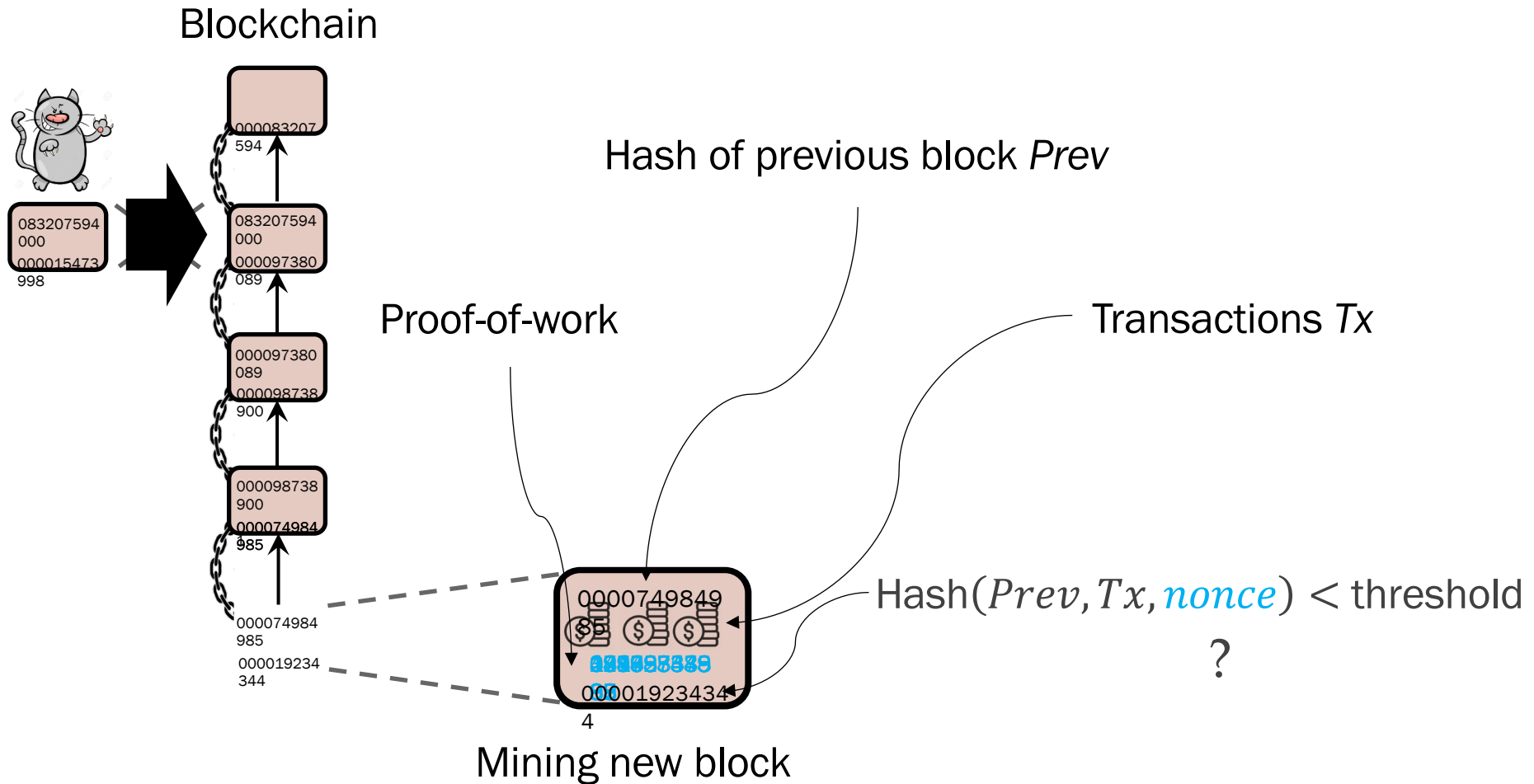
# Mining rule

Blockchain

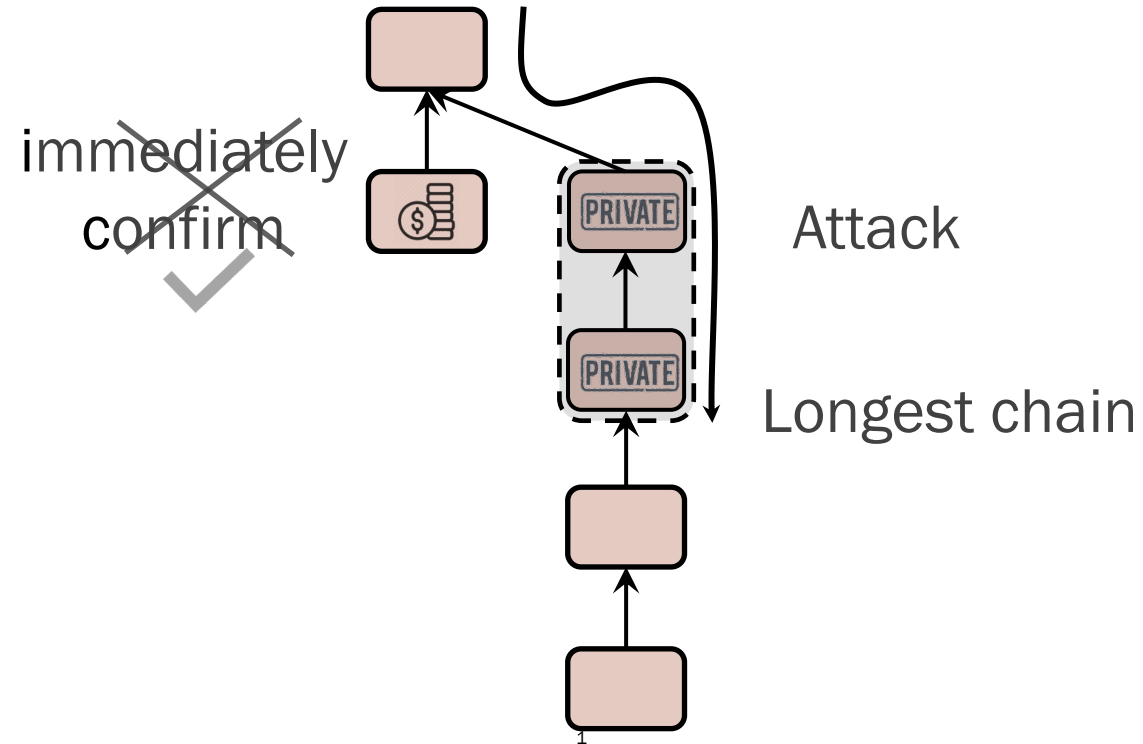


- Mining on the longest chain
- Poisson arrivals of blocks
- Average mining rate  $\lambda = 1$  block per 10 min

# Proof-of-Work



# Instant confirmation

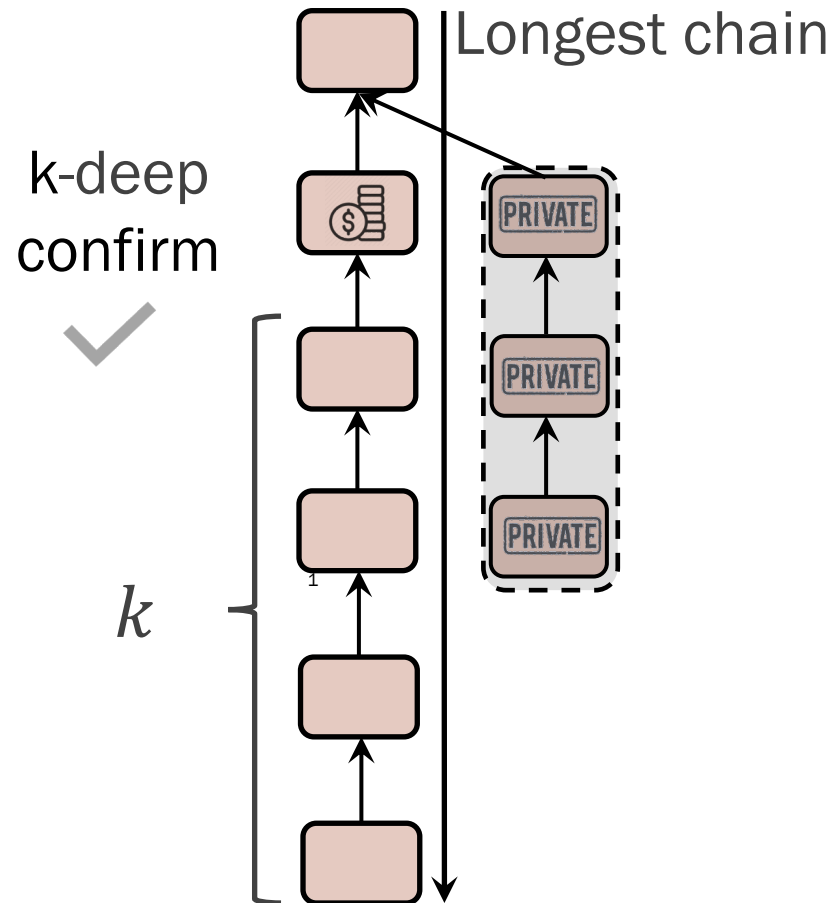


# k-deep confirmation

30% adversary power

k=0  $\varepsilon = 1.0000000$   
k=5  $\varepsilon = 0.1773523$   
k=10  $\varepsilon = 0.0416605$   
k=15  $\varepsilon = 0.0101008$   
k=20  $\varepsilon = 0.0024804$   
k=25  $\varepsilon = 0.0006132$   
k=30  $\varepsilon = 0.0001522$   
k=35  $\varepsilon = 0.0000379$   
k=40  $\varepsilon = 0.0000095$   
k=45  $\varepsilon = 0.0000024$   
k=50  $\varepsilon = 0.0000006$

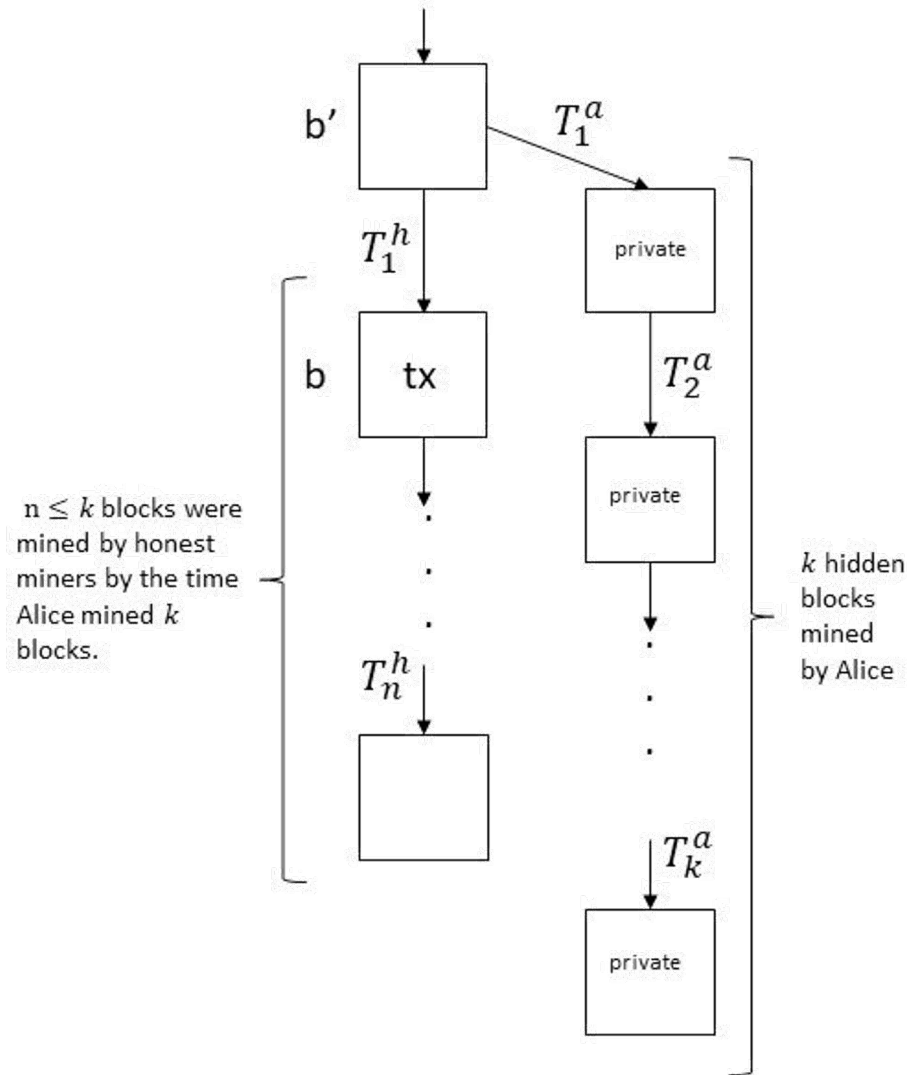
Nakamoto's table



# Notations

- total mining rate  $\lambda$
- honest mining rate  $\lambda_h$
- adversarial mining rate  $\lambda_a$
- adversarial fraction  $\beta$
- network delay bound  $\Delta$ . (assumed 0 for now)

# Private attack analysis

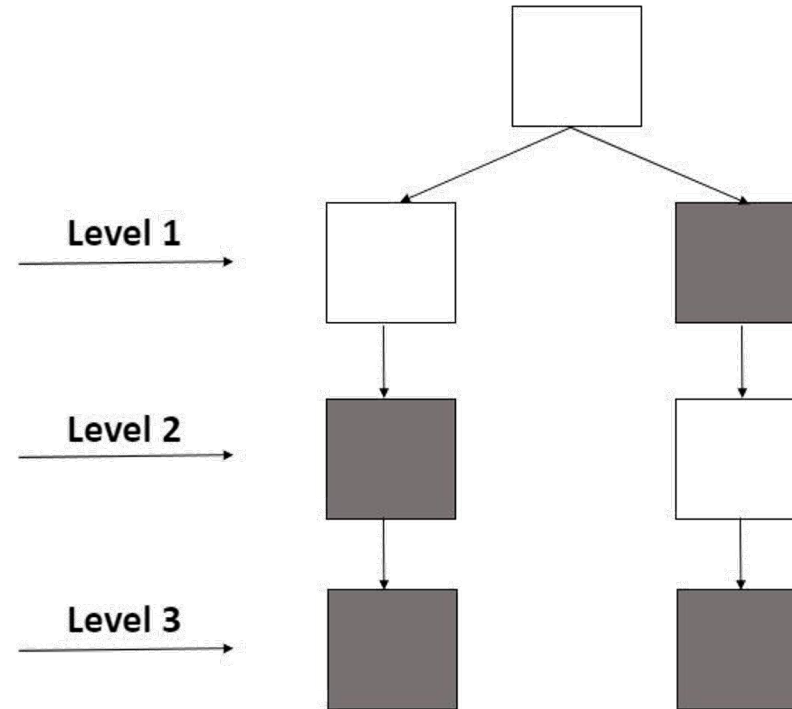


# Safety

- A block  $b$  is **safe** if once it is confirmed, it remains on the ledger in the view of any node at any future time.....regardless of the adversary's attack.
- What we showed is safety with high probability.....under a specific attack, the private attack.
- What about other attacks?

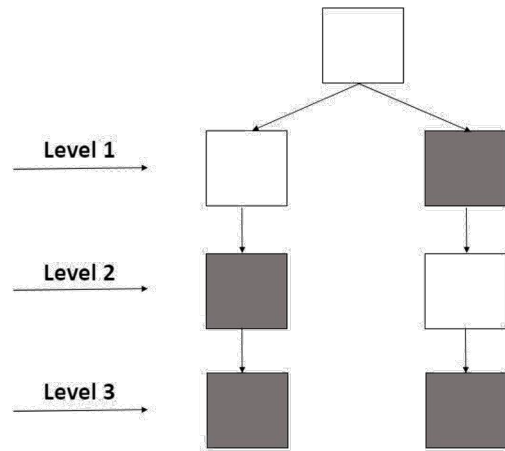


# Example: balance attack

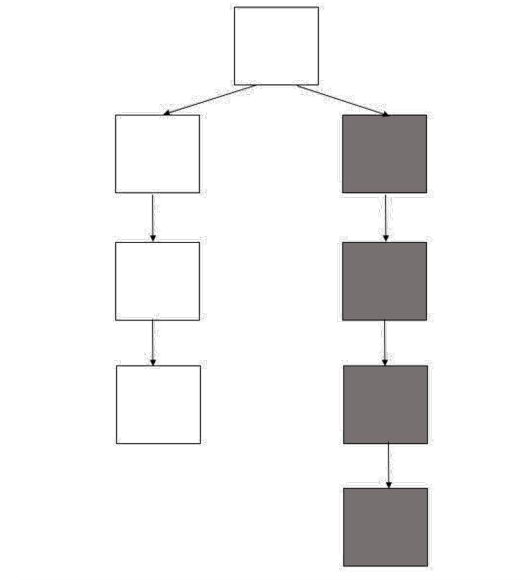


# Safety analysis (for level 1 block)

any successful attack



private attack



# Safety theorem for Bitcoin

Theorem:

Each Bitcoin block is safe with probability of confirmation error going to zero exponential in  $k$  if  $\lambda_a < \lambda_h$

# Is Safety Enough?

- What happens if no honest blocks are confirmed?
- We need liveness.
- A protocol is **live** if a non-zero fraction of honest blocks are confirmed.

# **Bitcoin: chain growth and chain quality**

# Bitcoin: liveness theorem

Theorem:

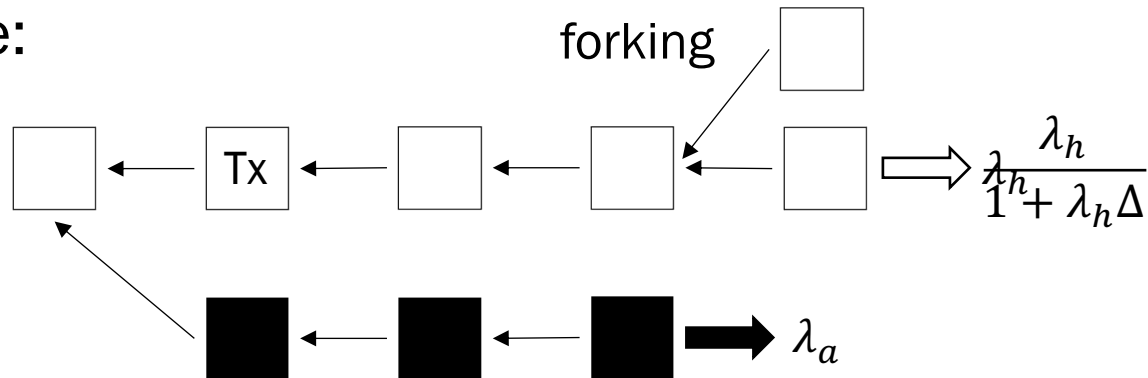
Bitcoin is live if  $\lambda_a < \lambda_h$

# Network delay

- So far we have assumed communication of blocks happen instantaneously.
- But real networks have delays.
- Synchronous model: communication of all blocks is delayed by at most  $\Delta$  seconds.

# Private attack analysis

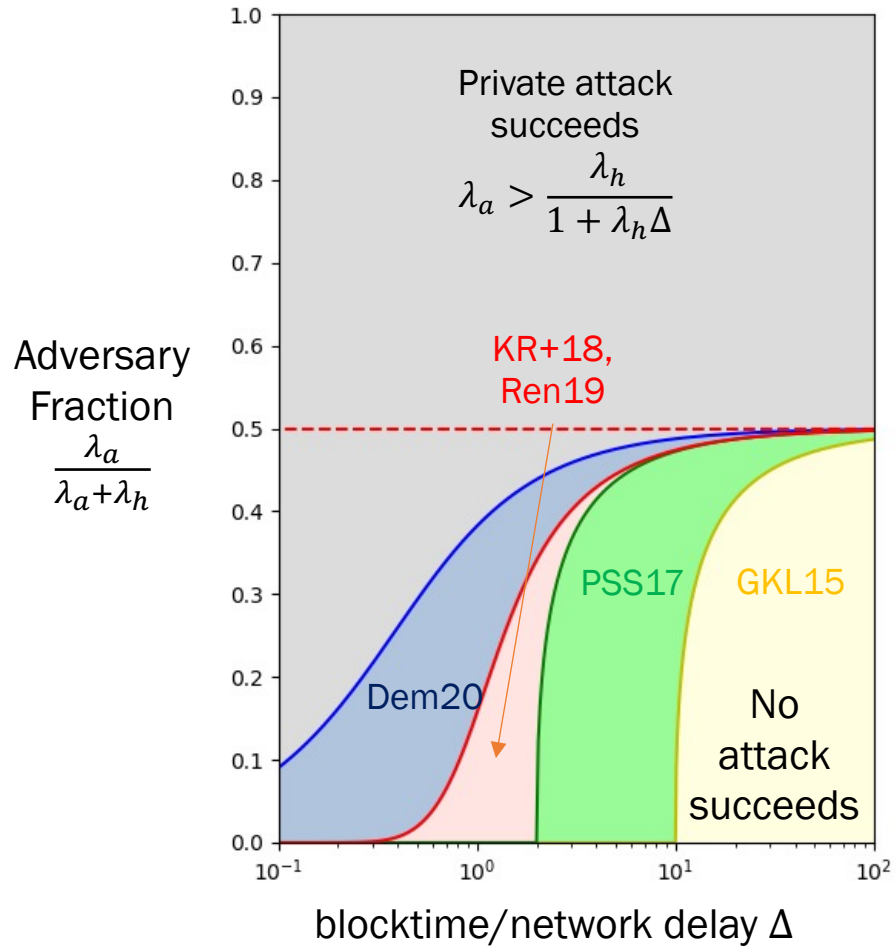
The race:



Private attack succeeds if  $\lambda_a > \frac{\lambda_h}{1 + \lambda_h \Delta}$



# What about all attacks?



# **Part III:**

# **Speeding up Bitcoin**

V. Bagaria, S. Kannan, D.T., G. Fanti, P. Viswanath, “Prism: Deconstructing the blockchain to approach physical limits “, ACM CCS’19.

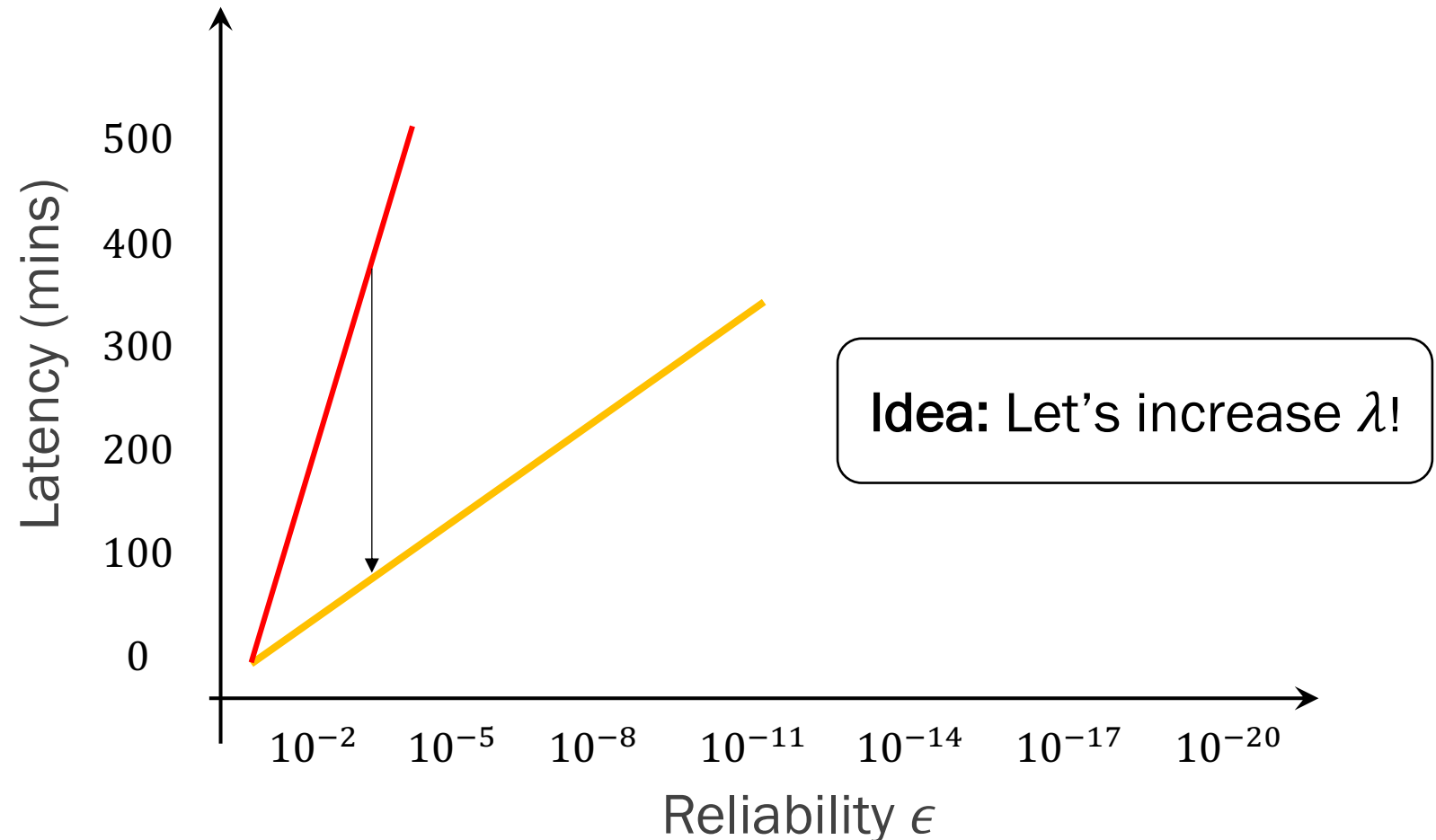
# Confirmation latency

Mining rate  
 $\lambda = 1$  block/10 min

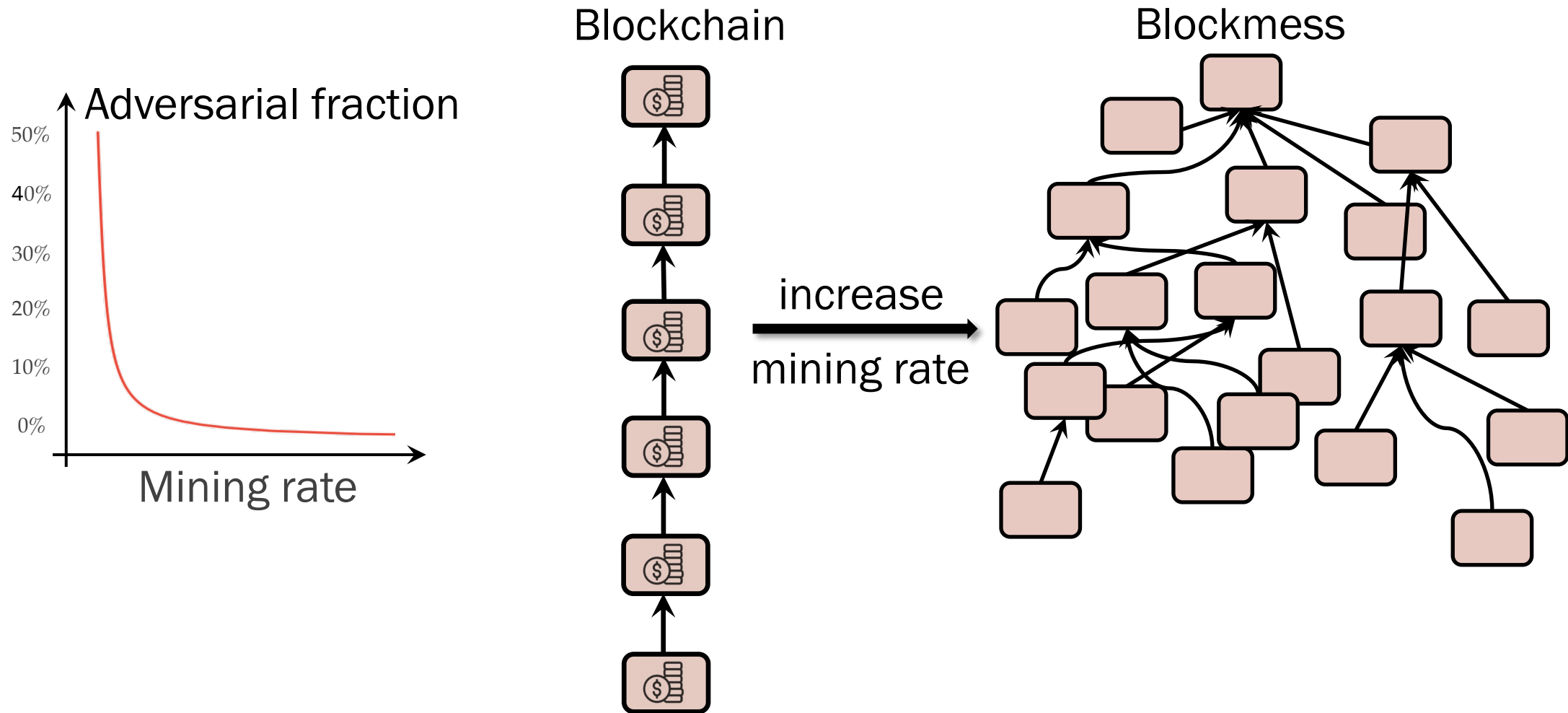
30% adversary power

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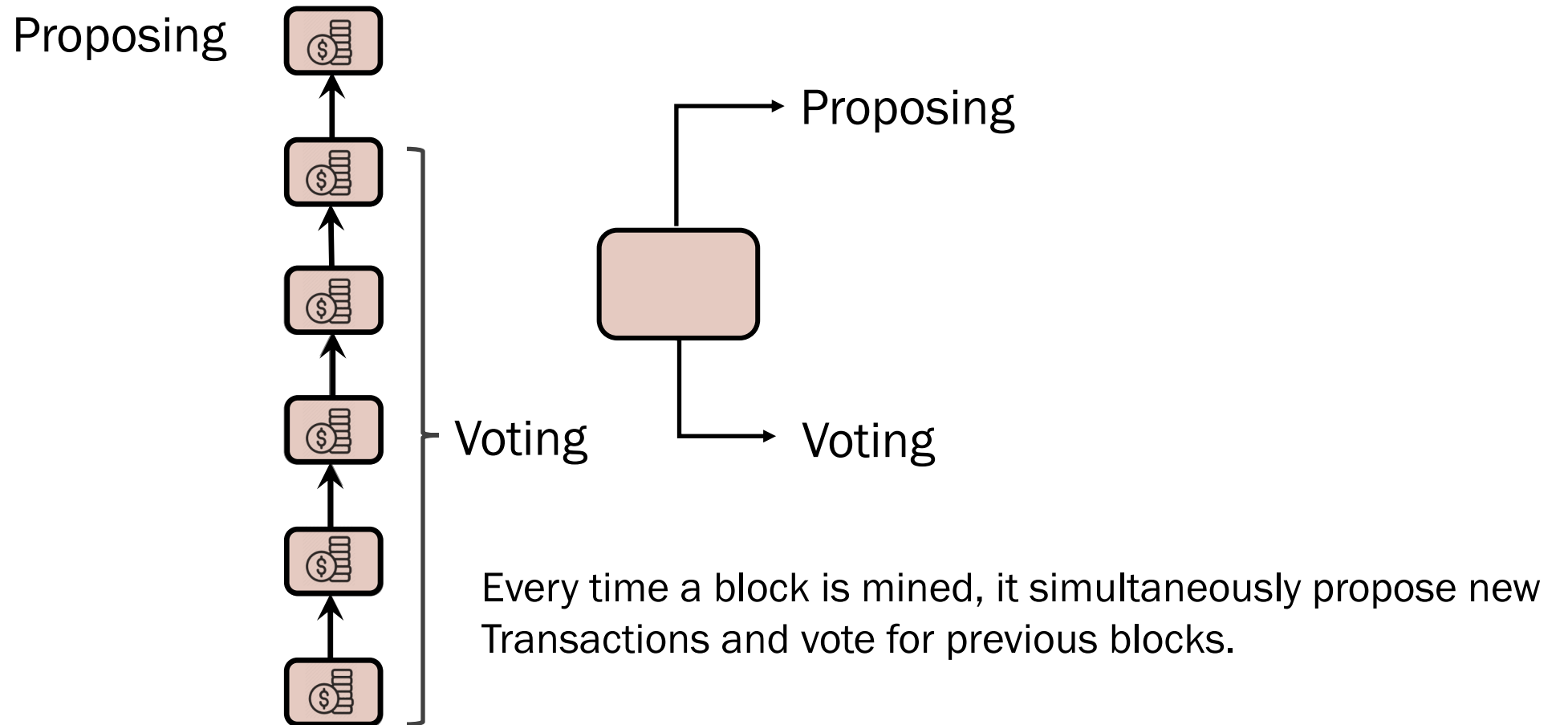
Nakamoto's table



# Scale the mining rate



# 2 roles of a Bitcoin block

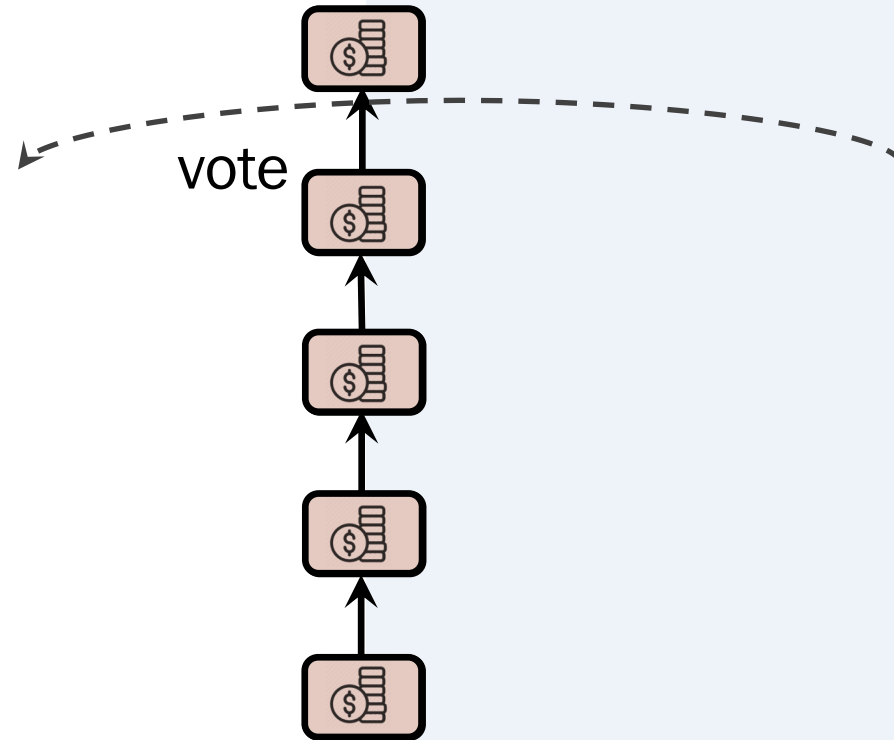


**Deconstruct Bitcoin, and scale.**

# Bitcoin → Deconstruct

Proposing

Voting



# Bitcoin → Deconstruct → Scale

Many parallel PoW lotteries: Proposing

2-for-1 mining [GKL15,PS17]

Proposing and voting:

1. Segregated by proposer block heights.
2. Each voter tree votes for the first seen proposer block at each height,
3. Only **votes** from main chains count.
4. For each height choose the proposer block with most votes.



votes

Voting



Many voter trees

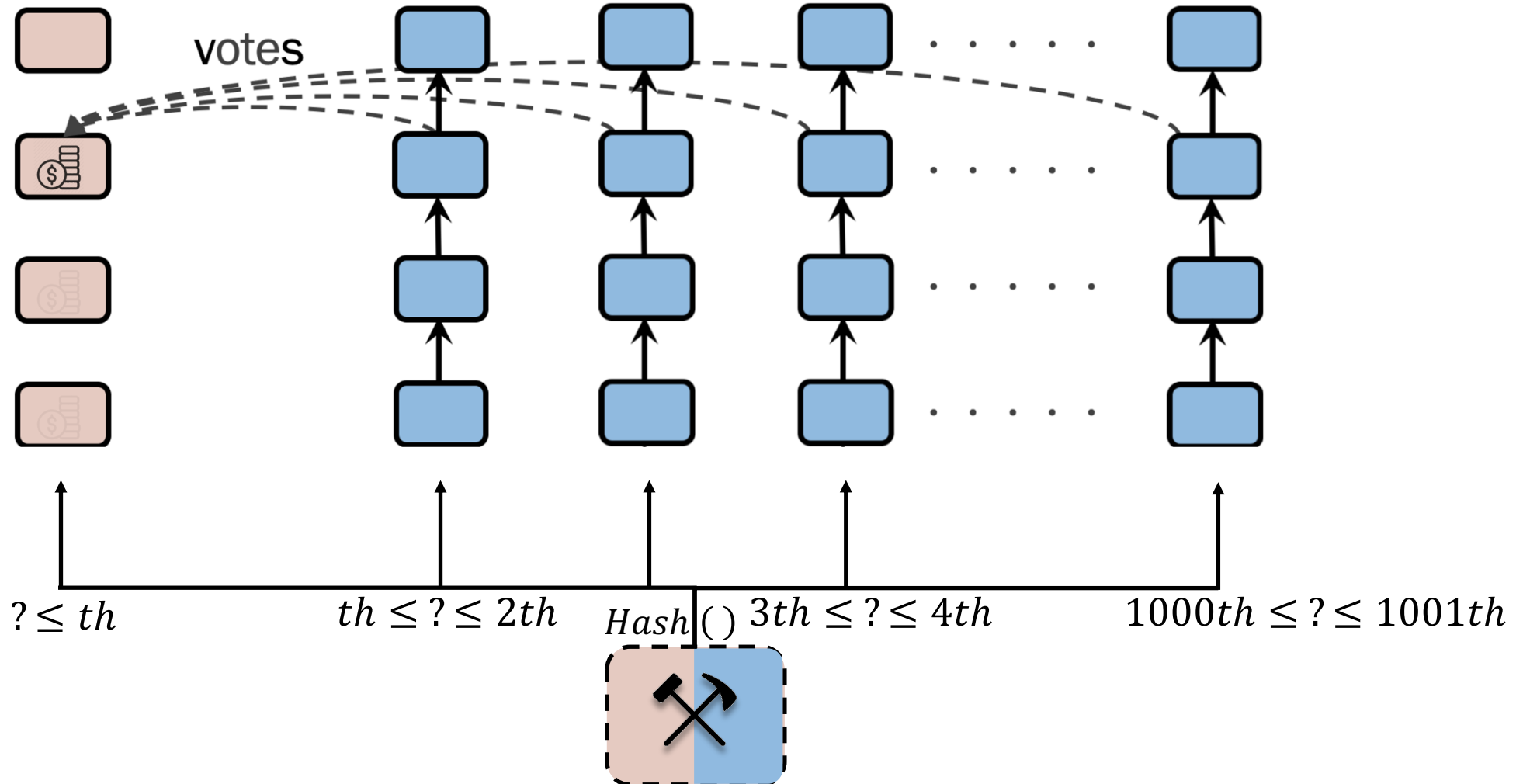




# Prism: Mining

Proposer Tree

1000 Voter Trees



# Theorems

## Security

*Prism* achieves safety and liveness against an adversary with less than 50% of total hash power.

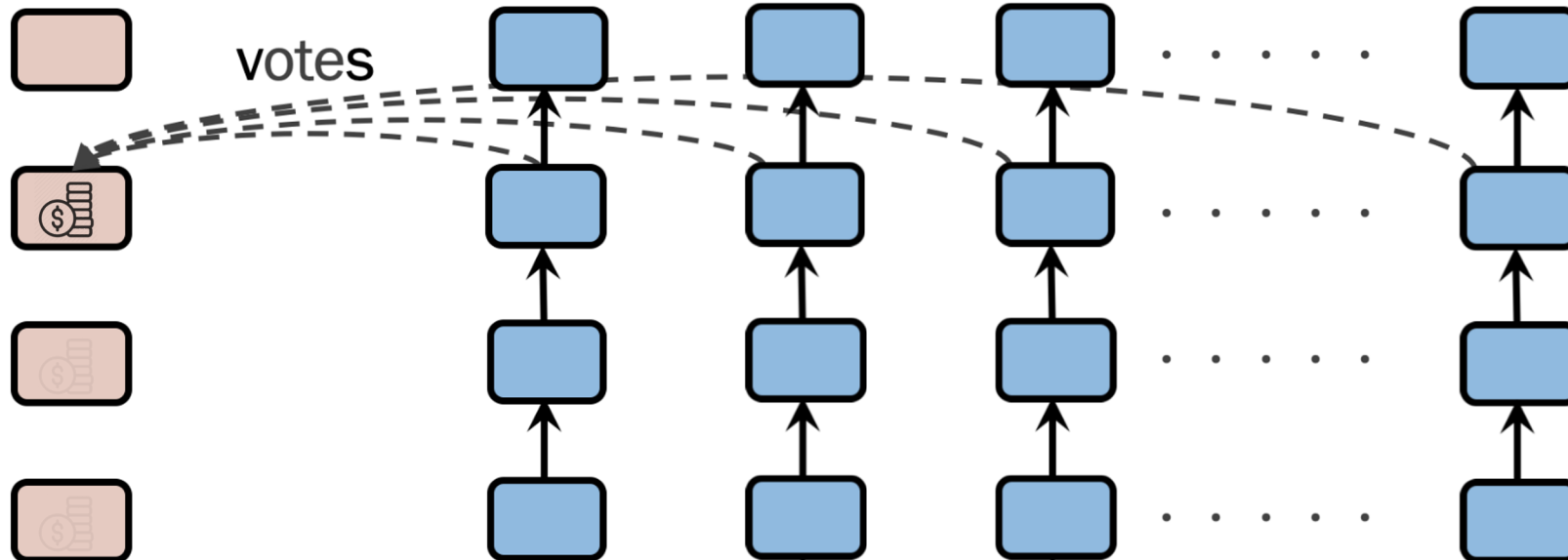
## Normal-path Latency

*With probability  $1 - \epsilon(m)$ , Prism confirms transactions with constant average latency, independent of  $m$ , # of voter chains.*

# Prism: Safety and Liveness

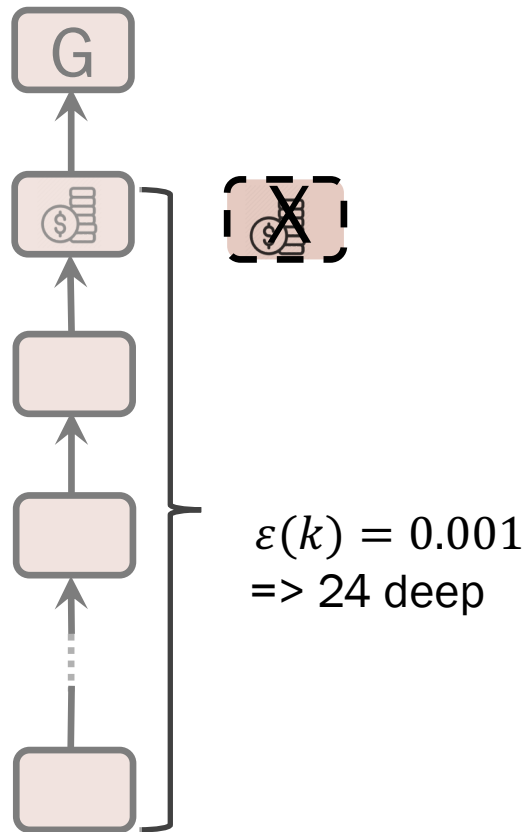
Proposer Tree

1000 Voter Trees

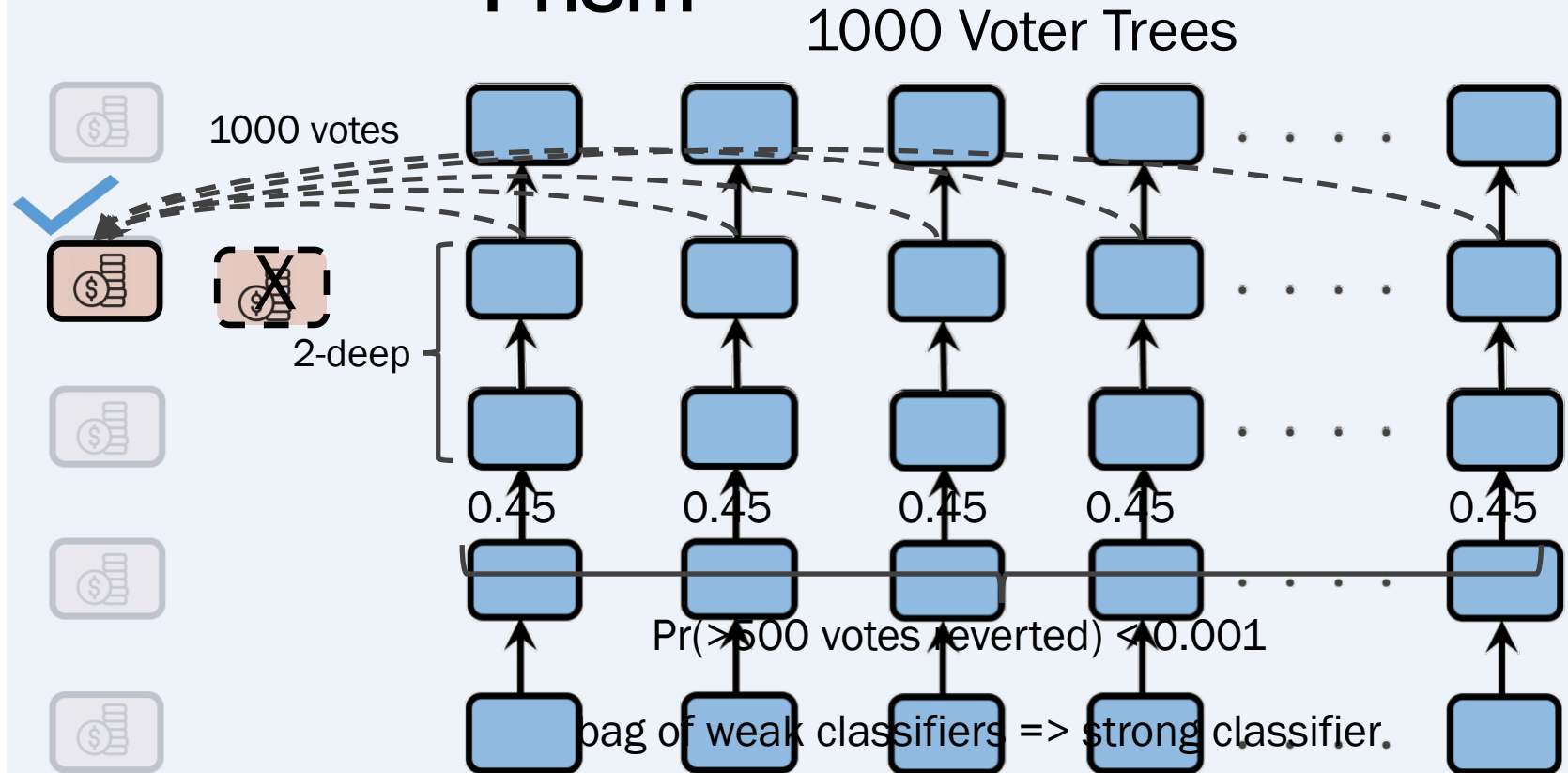


# Prism: fast confirmation

## Bitcoin



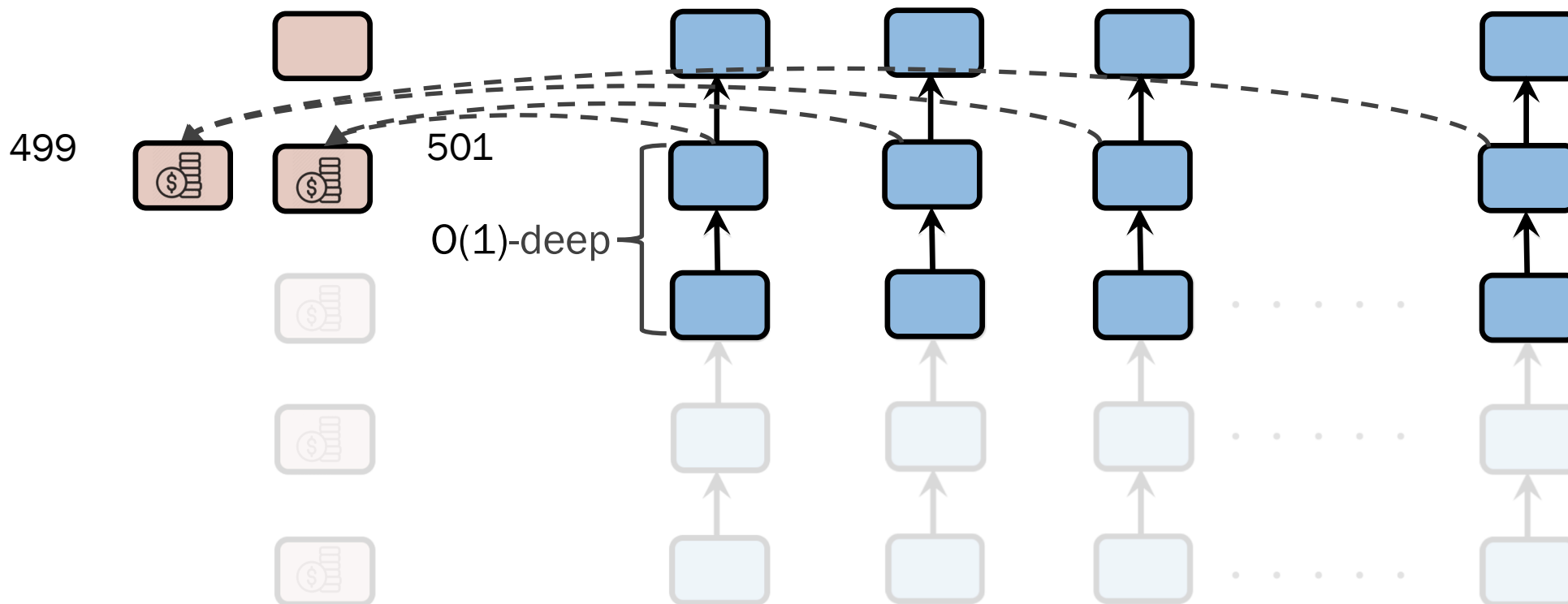
## Prism



# Multiple proposer blocks

Proposer Tree

1000 Voter Trees



# Multiple proposer blocks

Proposer Tree

1000 Voter Trees



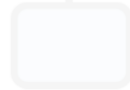
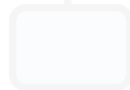
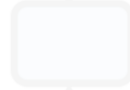
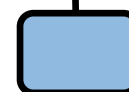
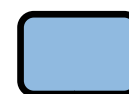
499

$A \rightarrow B:10$   
 $C \rightarrow D_1:10$

$C \rightarrow D_2:10$   
 $A \rightarrow B:10$

501

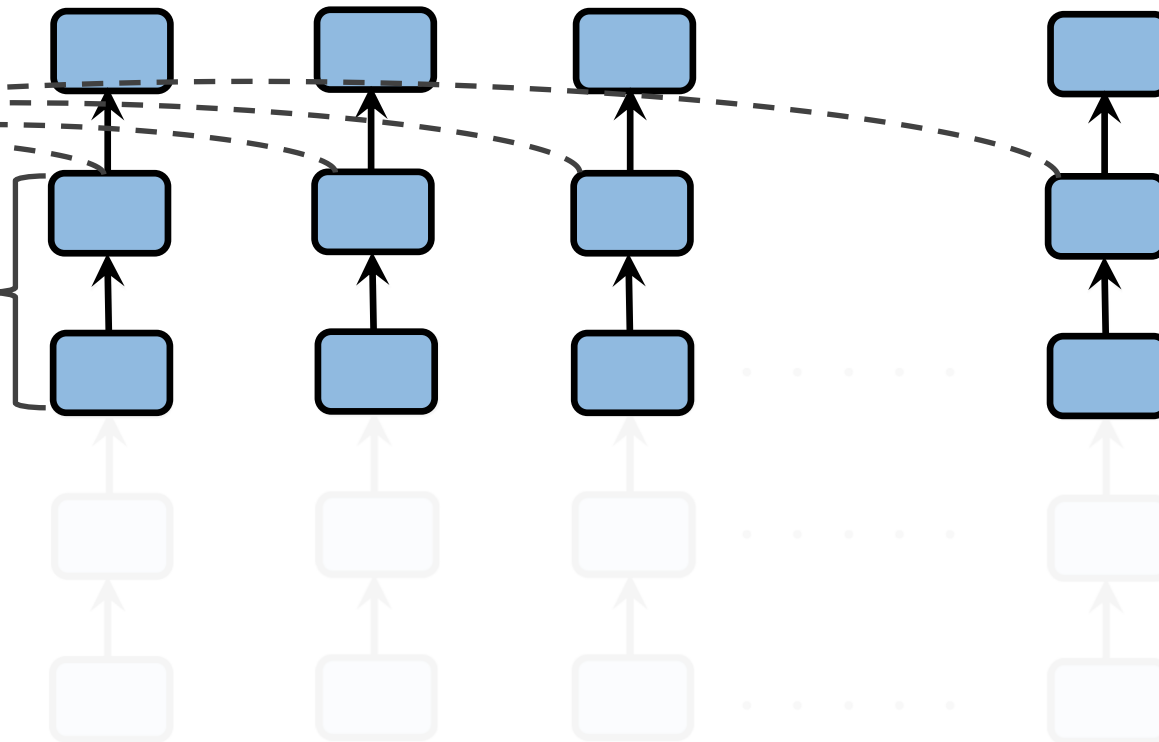
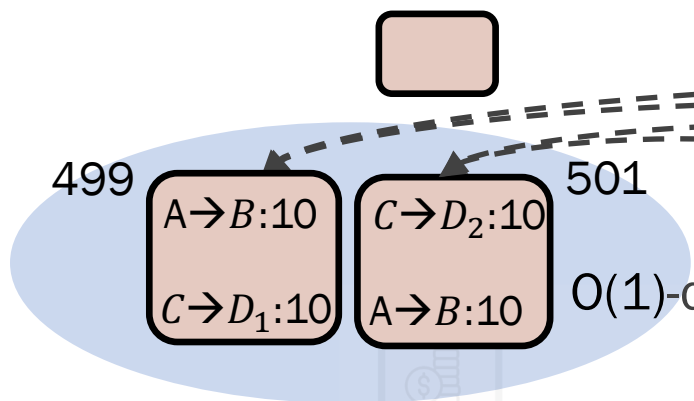
$O(1)$ -deep



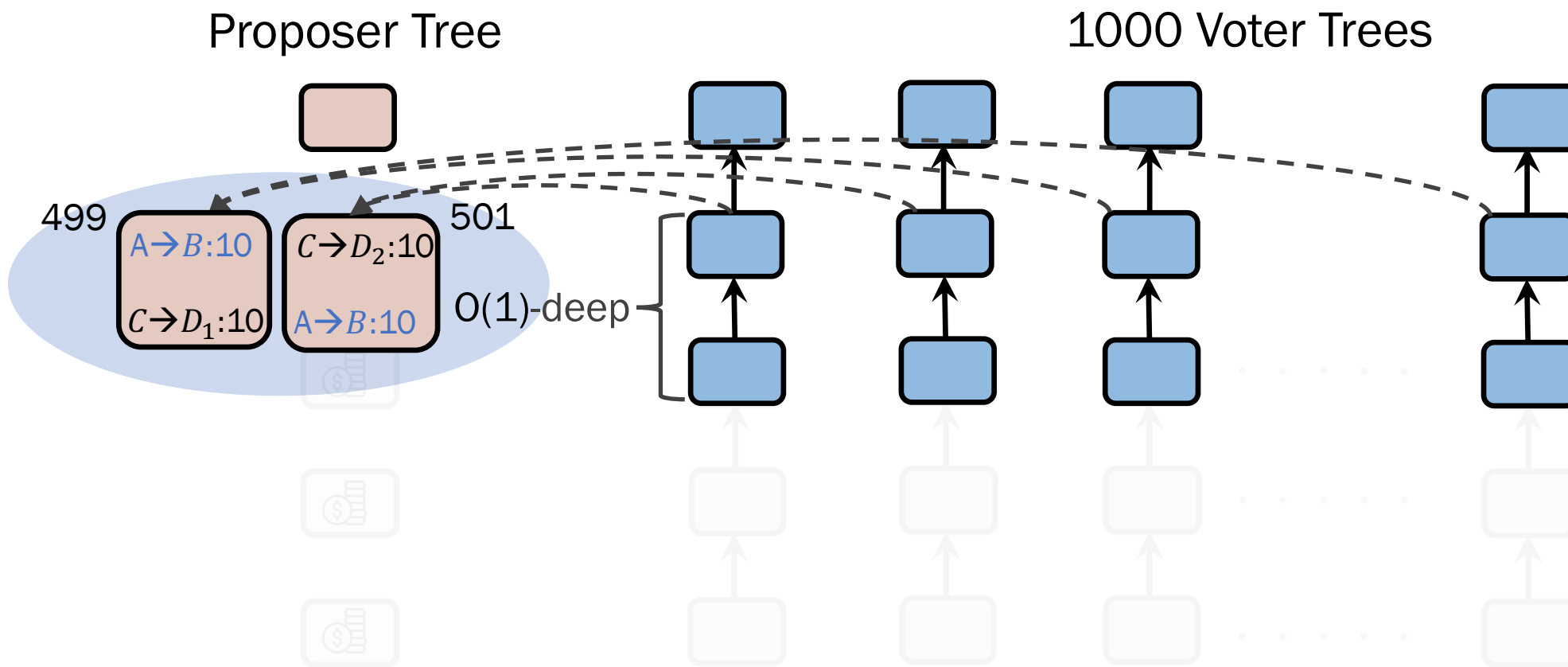
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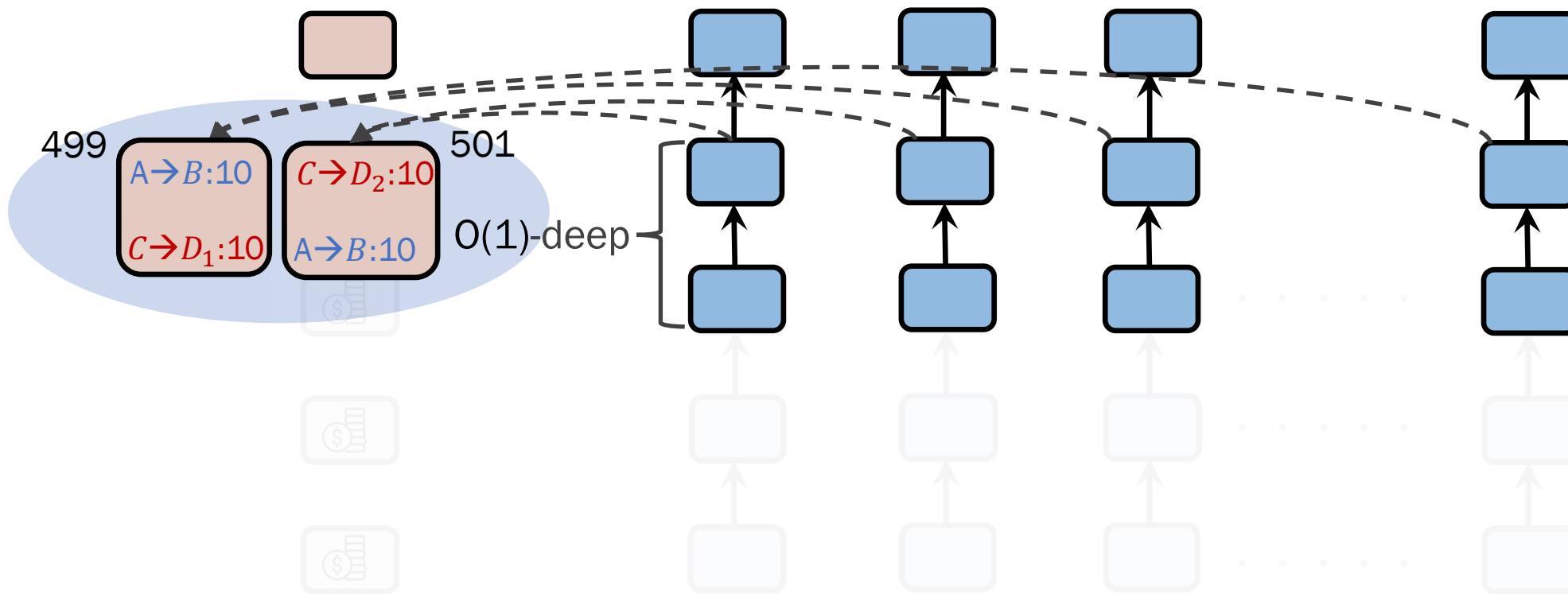
# Multiple proposer blocks



# Multiple proposer blocks

Proposer Tree

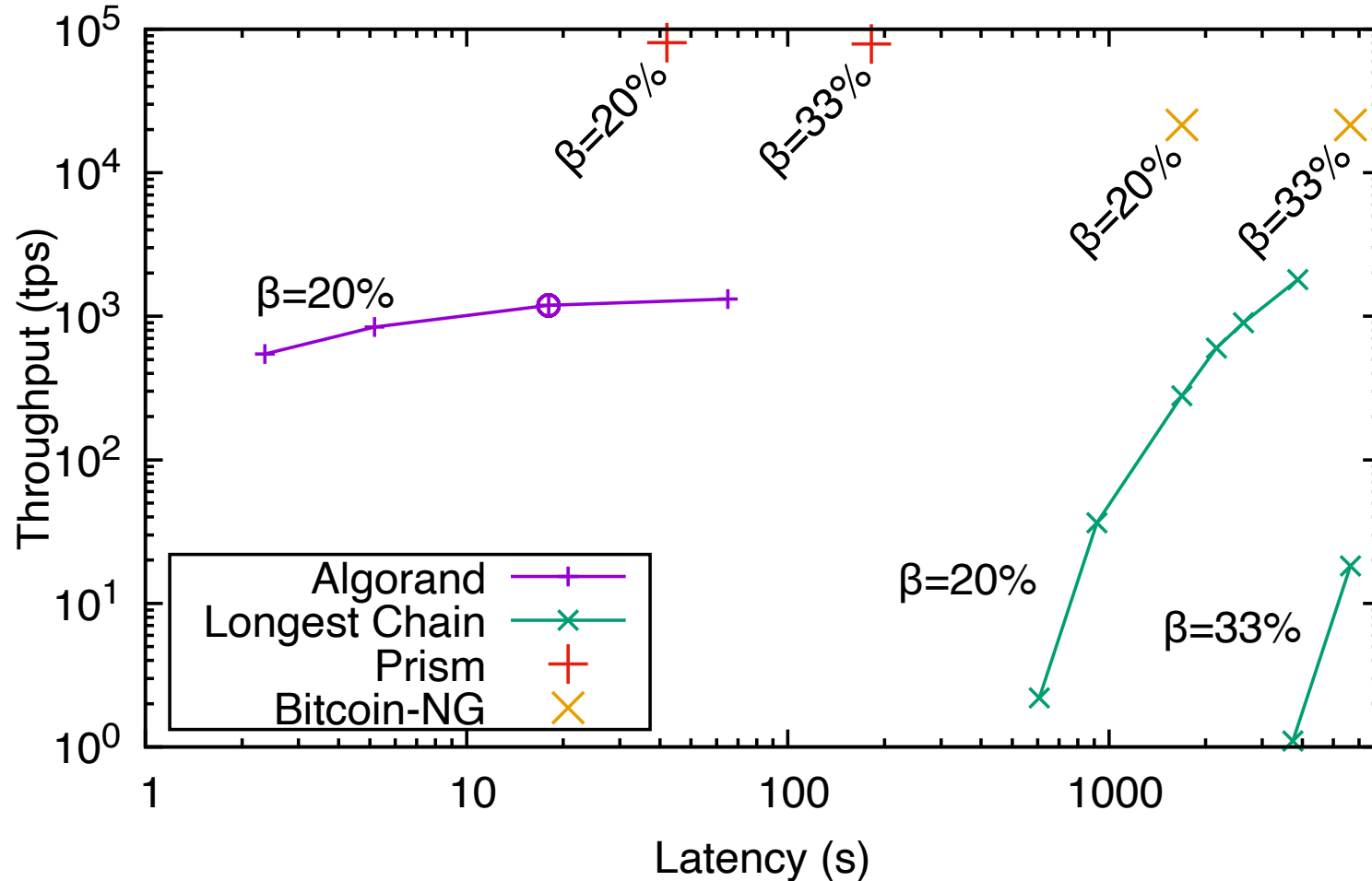
1000 Voter Trees





# Rust Implementation

4-regular topology of 100 EC2 c5d.4xlarge instances, 120ms delay, 400 Mbps bandwidth per link.



Yang et al, "Prism: Scaling Bitcoin 10,000 X", arXiv:1810.08092